

Other Things From Chapter 8

Combination - order doesn't matter $C(n,r) = n!/(n-r)!r!$

Permutation - order matters $P(n,r) = n!/(n-r)!$

The Binomial Theorem

In the expansion of $(x+y)^n$

$$(x+y)^n = x^n + nx^{n-1}y + \dots + {}_nC_r x^{n-r}y^r + \dots + nxy^{n-1} + y^n$$

The coefficient of $x^{n-r}y^r$ is

$${}_nC_r = n!/(n-r)!r!$$

The symbol $\binom{a}{b}$ is often used in place of ${}_nC_r$ to denote binomial coefficients.

Ex. Find the binomial coefficient.

a) ${}_8C_2 = 8!/(8-2)!2! = 8!/6!2! = 8 \cdot 7/2 = 28$

b) $(10/3) = 10!/(10-3)!3! = 10!/7!3! = 10 \cdot 9 \cdot 8/3 \cdot 2 \cdot 1 = 120$

The Binomial Coefficient (Pascal's Triangle)

$$(x+y)^0 = 1$$

$$(x+y)^1 = x+y$$

$$(x+y)^2 = x^2 + 2xy + y^2$$

$$(x+y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

... and so on.

Sums of Powers of Integers

1. $\sum_{i=1}^n i = 1+2+3+4+\dots+n = n(n+1)/2$

2. $\sum_{i=1}^n i^2 = 1^2+2^2+3^2+4^2+\dots+n^2 = n(n+1)(2n+1)/6$

3. $\sum_{i=1}^n i^3 = 1^3+2^3+3^3+4^3+\dots+n^3 = n^2(n+1)^2/4$